Water-Assisted Increase of Ionic Conductivity of Lithium Poly(acrylic acid)-Based Aqueous Polymer Electrolyte

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ABSTRACT: We propose a novel aqueous polymer electrolyte (APE) using a strongly hydrophilic poly(acrylic acid) (PAA) matrix containing mobile lithium counterions. The conductivity of this new PAA–Li⁺–water electrolyte increases dramatically (to $10^{-2}$ S/cm at 298 K) with the addition of water. This value is almost 100 times higher than those of nonaqueous electrolytes and solid-state electrolytes. From the molecular dynamics simulations, we find that the increase of ion conductivity originates from the close interplay between ions, water, and the polymers in the molecule level. The structural features (i.e., ion/water distribution around the polymer) and transport properties (i.e., diffusion coefficient and ionic conductivity) are systematically investigated along with the quantifications of the microscopic properties such as the binding index of the ion, hydration numbers, and the equilibrium distance between the ion and PAA monomer at various water-content conditions. In particular, the change in the conductivity according to water content, $\phi_{Wt}$, is divided into the diffusion-dominant regime at the low-water-content condition ($\phi_{Wt} < 0.7$) and the structure-dominant regime at the high-water-content condition ($\phi_{Wt} \geq 0.7$). In the diffusion-dominant regime, the conductivity increases by diffusion enhancement proportional to the water content, while in the structure-dominant regime, the conductivity varies little due to the considerable reduction of the number density of Li ions. Namely, there exists an optimal water content, above which the effects of additional water become negligible. We believe that our innovative findings would provide significant advances in developing APE-based high-power and long-life lithium-ion batteries. Also, the proposed nontoxic and flexible APE could offer a promising solution for the development of flexible and wearable aqueous rechargeable lithium-ion batteries.

KEYWORDS: aqueous polymer electrolyte, ionic conductivity, ionic diffusion, diffusion-dominant regime, structure-dominant regime, binding index, ion–water interaction, ion hydration structure

1. INTRODUCTION

Since first commercialized by the Sony Corporation in 1991, the performance of lithium-ion batteries (LIBs) has been tremendously improved.1–3 As a result, they are currently utilized as energy storage for diverse high-technology applications such as mobile phones, laptops, and electric vehicles.4 However, there still exists an unresolved conflict with LIBs: a high-performance electrolyte versus safety. The organic-solvent-based liquid electrolytes used in conventional LIBs provide superior conductivity, one of the key factors for a high-performance battery, but this performance often comes with toxicity, volatilization, flammability, and explosions when such batteries are used under extreme conditions.5 Those safety concerns could be avoided by replacing flammable liquid electrolytes in LIBs with solid-state electrolytes (SSEs). However, except several sulfide solid-state electrolytes, most SSEs have inherently lower ionic conductivity than liquid electrolytes do; therefore, current efforts are focused on improving their conductivity.5 As one option to overcome these challenges, aqueous polymer electrolytes (APEs) have recently attracted considerable attention. This is due to their particular combination of advantages as an aqueous electrolyte (nonflammability, environmental friendliness, moisture insensitivity, and low cost)6,7 and a polymer matrix (leakage-free feature, structural integrity, and flexible design possibility).8 These characteristics make them ideal choices for use, even in wearable electronics.

In this study, we introduce a new single-ion Li⁺-conducting APE and focus on the enhancement of the APE conductivity. The continuous addition of water to an APE that initially consists only of a polyanion matrix and lithium counter cations

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Na+, as the medium is hydrated, its conductivity was reported containing Silica Nanoparticles comparable to or higher than those of the aqueous electrolytes (NEs) and NE-based SSEs, and they are lithium single-ionic conductivities in this APE (>10^-3 S/cm) when an appropriate amount of water is added. This is found out in the interplay between polymers, ions, and water that occurs as the amount of water varies. For example, what is the influence of the ion—water structure around polymers on the conductivity? How does the hydration number of ions vary with the addition of water?

**2. EXPERIMENTAL SECTION**

**2.1. Experimental Procedure.** For the experimental system, we prepared lithium single-ion-conducting PAA-based APEs containing silica nanoparticles, where PAA and silica nanoparticles act as the polymer matrix and chemical cross-linking points, respectively. Electrochemical impedance spectroscopy provided direct information about the ionic conductivity in the electrolytes with various water weight fractions \( \phi_{w} = 0.3 \) to 0.9. Also, Figure S1 in the Supporting Information shows an example of the typical conductivity spectra, where the ionic conductivity value was obtained from the in-phase part of the conductivity.

**2.2. Materials and Synthesis of APEs.** Li^+ single-ion-conducting PAA-based APEs containing silica nanoparticles were synthesized via two-step processes (see Scheme 1), such as a sol–gel reaction and free radical polymerization. The sol–gel method was used to prepare vinyl silica nanoparticles (VSNs) acting as covalent cross-linking points (see Scheme 1(a)), thereby allowing for the creation of a solid-state network structure. Vinyltrithiolsilane (1.9 g, Tokyo Chemical Industry) was added into deionized water (15 mL). Then, the mixture was allowed to react overnight at room temperature, resulting in VSNs (whose average diameter is around 5 nm as shown in Figure S2 in the Supporting Information) dispersed in water. A solution of AA monomers (0.6 g, Sigma-Aldrich) in deionized water (1.4 mL) was added to the VSN dispersion solution (0.15 g). The mixture was stirred for 1 h, and then, ammonium persulfate (APS, 0.02 wt %, Alfa Aesar) as the initiator was added to the aqueous mixture. The temperature of the reaction mixture was maintained under 70 °C for 3 h to give a transparent solid-state VSN cross-linking PAA membrane (Scheme 1(b)). To neutralize the PAA membrane with Li^+, the product was soaked in a mixed solution of lithium hydroxide (LiOH, 1 g, Tokyo Chemical Industry) and methanol (MeOH, 100 mL, Duksan Reagents) for 5 days and then washed several times with MeOH and filtered to remove any unreacted LiOH. The Li^+-neutralized PAA membrane was dried at 40 °C for overnight to completely remove the solvent. The extent of neutralization (99% neutralized with Li^+) achieved from the ion exchange procedure was confirmed by elemental analysis from inductively coupled plasma mass spectrometry and pH value analysis (Figure S3). The various amounts of deionized water (31, 51, 67, 82, 85, and 89 wt %, listed in Table S1) were added to the sample to demonstrate the effect of water content on ionic conductivity. The additionally detailed experimental analyses of these materials were conducted using the
rheological, thermal, and microstructural measurements. The Supporting Information contains the information on the PAA spacing between the silica nanoparticles (Mw ≈ 90 100 g/mol, Figure S4), glass transition temperature (Tg = 102 °C, Figure S5), silica nanoparticle distribution within the PAA matrix (Figure S6), and pH value (~6.36, Figure S7).

2.3. Ionic Conductivity Measurement. The ionic conductivity measurements of the APEs were performed by electrochemical impedance spectroscopy using a Bio-Logic VSP-300 multipotentiostat, with a 10 mV amplitude and 10⁻⁵~10⁻⁷ Hz frequency range. Samples were prepared by sandwiching them between two freshly polished brass top and bottom electrodes with 10 and 20 mm diameters, respectively. This created a parallel plate capacitor cell, and its precise thickness verification proceeded after the measurements were completed. Data were collected in isothermal frequency sweeps at room temperature. The complex dielectric ε*(ω) = ε′(ω) – iε″(ω) and conductivity [σ*(ω) = σ′(ω) + iσ″(ω)] functions were obtained by measuring the complex impedance [Z*(ω)] and given by

\[
\varepsilon'(\omega) = \frac{1}{C_0} \frac{1}{i\omega Z'(\omega)} = \frac{L}{A\varepsilon_0} \frac{1}{i\omega Z''(\omega)}
\]

\[
\sigma'(\omega) = \frac{1}{\omega \varepsilon_0} \sigma''(\omega)
\]

where C0 is the vacuum capacitance, ω is the angular frequency, ε0 is the vacuum permittivity, L is the distance between the electrodes, and A is the cross-sectional area of the top electrode. The ionic conductivity σ_\text{app} is noted as the plateau region in the in-phase part of conductivity σ′(ω) as indicated by the dashed horizontal line in Figure S1.

3. MOLECULAR DYNAMICS SIMULATIONS

Along with the in situ experimental observation, the extensive MD simulations were performed to understand the mechanism of conductivity of the PAA–Li⁺–water electrolyte. Figure 1 presents the molecular visualization of the PAA–Li⁺–water electrolyte system used in this study at a representative water content of ϕ_{Wt} = 0.7. The water content, ϕ_{Wt} is the mass fraction of water in the system, and it is expressed as

ϕ_{Wt} = \frac{m_{Wt}}{m_{\text{PAA}} + m_{Wt} + m_Li}

where m_{\text{PAA}}, m_{Wt}, and m_Li are the mass of PAA, water, and the lithium ion, respectively. In all the MD simulations, the number of PAA molecules and Li ions (Li⁺) are kept constant as 27 and 2484, respectively. Each PAA molecule has 92 periodic monomers. The number of Li⁺ was determined for the present system is discussed in Supporting Information, Figure S8.

Simulation was proceeded for 40 to 90 ns more to produce the data. The time step for the simulations was 1.0 fs.

4. RESULTS AND DISCUSSION

4.1. Ionic Conductivity. Figure 2(a) shows a comparison between the conductivities from experiments, σ_{exp}, and those from MD simulations, σ_{MD}, at various ϕ_{Wt}. The ionic conductivity from MD simulations, σ_{MD}, was computed from the Nernst–Einstein relation,

\[
\sigma_{\text{MD}} = \frac{n_{Li} e^2 D_{Li}}{k_B T}
\]

where n_{Li} and D_{Li} are the number density and diffusion coefficient of Li ions, respectively, T is the system temperature, e is the elementary charge, and k_B is the Boltzmann constant. This formula indicates that the conductivity of an electrolyte is determined by n_{Li} and D_{Li}. Here, n_{Li} is the system ion concentration, which is associated with the microscopic structure of the electrolyte, while D_{Li} expresses the dynamics of ion mobility. The validity of Nernst–Planck relation in the present system is discussed in Supporting Information, Figure S8.

As observed in Figure 2(a), σ_{MD} agrees very well with σ_{exp}, which confirms the validity of the present MD simulations. Thus, all the discussion in this study is based on the MD simulation results. When the water content is small (ϕ_{Wt} = 0.1), the ionic conductivity is also relatively small (σ_{MD} = 2.84 ± 0.20 × 10⁻⁴ S/cm). However, the conductivity increases...
with the addition of water and reaches \( \sigma_{\text{MD}} = 1.29 \pm 0.014 \times 10^{-2} \, \text{S/cm} \) at \( \phi_{\text{Wt}} = 0.7 \). For \( \phi_{\text{Wt}} \geq 0.7 \) the increment in \( \sigma_{\text{MD}} \) becomes insignificant, which is still consistent with \( \sigma_{\text{exp}} \). Hence, the entire MD conductivity profile can be divided into two distinctive regimes, and each section is fitted with a linear line in a log–linear plot (see the dashed lines A and B in Figure 2(a) and eq S1 in the Supporting Information).

Figure 2(b) shows the change of \( n_{\text{Li}} \) according to \( \phi_{\text{Wt}} \). Here, \( n_{\text{Li}} \) is a quantity averaged over the whole system. As \( \phi_{\text{Wt}} \) increases, \( n_{\text{Li}} \) decreases. The increase in \( \phi_{\text{Wt}} \) brought the expansion of the simulation box, and the box dimensions were determined spontaneously through an equilibrium MD simulation with the NPT ensemble at \( p = 1.0 \, \text{atm} \) and \( T = 300 \, \text{K} \). In other words, the ion and water structures around the polymer were adjusted to minimize the total energy of the system, and a simulation domain with an optimized size was created while achieving equilibrium. When the amount of water in the system varies, the microstructures of ions and water near polymers are modulated in ways that form a new hydration configuration around ions. It leads to a local change in the specific volume of water, and new system dimensions and \( n_{\text{Li}} \) are settled.

Figure 2(c) reveals the change of \( D_{\text{Li}} \) depending on \( \phi_{\text{Wt}} \). The diffusion coefficient was determined as the slope of the MSD (mean-square-displacement) plot at long-time limit:

\[
D_{\text{Li}} = \lim_{t' \to \infty} \frac{(\langle r_{\text{Li}}(t) - r_{\text{Li}}(t') \rangle)^2}{6t'},
\]

where \( r_{\text{Li}}(t) \) is the instantaneous position of \( \text{Li}^+ \), \( t' \) the lag time, and \( \langle \cdots \rangle \) denotes an ensemble average—the MSD plots for all \( \phi_{\text{Wt}} \)'s are shown in Figure S9. Opposite to the behavior of \( n_{\text{Li}} \), \( D_{\text{Li}} \) increases in proportional to \( \phi_{\text{Wt}} \) in the log–linear plot.

From the observations of \( n_{\text{Li}} \) and \( D_{\text{Li}} \), we can conclude that the fast increase in conductivity for \( \phi_{\text{Wt}} < 0.7 \) is dominated by the diffusion, while the slow increase in the higher-water-content environment with \( \phi_{\text{Wt}} \geq 0.7 \) is due to a decrease in \( n_{\text{Li}} \). Therefore, in the present study, the low-water-content condition with \( \phi_{\text{Wt}} < 0.7 \) is referred to as the diffusion-dominant regime, while the water environment with \( \phi_{\text{Wt}} \geq 0.7 \) is denoted as the structure-dominant regime. In other words, the diffusion-dominant region and the structure-dominant region are solely distinguished based on the conduction behavior. As shown in Figure 2(a), in the range of \( \phi_{\text{Wt}} \geq 0.7 \), the increase in conductivity shrinks to be negligible, whereas the diffusion coefficient increases still apparently. Therefore, it can be thought that the sudden slow-down of increasing rate originates from the decrease in number density.

4.2. Binding Configurations between Li\(^+\) and PAA. A conventional approach to understanding the diffusion behavior of PAA–Li\(^+\)–water electrolytes is to consider the binding configurations between Li\(^+\) and PAA. In order to quantify the configuration, we introduce the binding index, \( N_{\text{bind}}^{\text{O}} \), which is defined as the number of PAA oxygen atoms bound to Li\(^+\). \(^{33}\) If the distance between a Li\(^+\) and a target oxygen atom in PAA is smaller than a critical value of \( d_{\text{eq}} = r_{\text{eq}} + \sigma_{\text{Li}-\text{O}} \), the Li\(^+\) is regarded as being bound to the oxygen atom. Here, \( r_{\text{eq}} \) is the equilibrium distance between the Li\(^+\) and oxygen atom in the PAA segment (COO\(^-\)) in the binding status. The value of \( r_{\text{eq}} \) is 0.208 nm, which was determined as the first peak position in the RDF for Li\(^+\) with respect to the oxygen atoms in PAA. \( \sigma_{\text{Li}-\text{O}} \) is the \( \sigma \)-value in LJ parameters for the Li\(^+\)–O pair. Figure 3(a) visualizes the Li\(^+\)–O binding configurations with diverse \( N_{\text{bind}}^{\text{O}} \)'s. In the bulk, the Li\(^+\) does not have any binding to PAA oxygen atoms, and \( N_{\text{bind}}^{\text{O}} \) has zero value. Note that four water molecules were displayed in Figure 3(a) with \( N_{\text{bind}}^{\text{O}} = 0 \), since the average hydration number of Li\(^+\) in bulk is about 4.\(^{11,12}\) However, as Li\(^+\) approaches to PAA, a binding is formed, and \( N_{\text{bind}}^{\text{O}} \) becomes nonzero. In the Li\(^+\)–O binding with \( N_{\text{bind}}^{\text{O}} = 1 \), the ion wanders freely around oxygen atom while keeping a
constant distance. For \( N_{O}^{\text{bind}} = 2 \), the Li ion is bound to two oxygen atoms from the same PAA monomer. However, for \( N_{O}^{\text{bind}} > 2 \), the ion is surrounded by multiple adjacent PAA segments. If a Li\(^+\) has \( N_{O}^{\text{bind}} = 3 \), three adjacent COO\(^-\) groups participate in the binding, and each group supplies one oxygen only. If the binding index is large like \( N_{O}^{\text{bind}} = 4 \), the oxygen atoms can be from different PAA monomers. For the present system, the bindings in which \( N_{O}^{\text{bind}} > 6 \) are hardly found. Since the binding between Li\(^+\) and PAA is formed through Li\(^+\)–O bindings, \( N_{O}^{\text{bind}} \) also represents the binding strength between Li\(^+\) and PAA polymer. In the present work, the Li ions in the system were regrouped as free Li\(^+\) with \( N_{O}^{\text{bind}} = 0 \) and bound Li\(^+\) with \( N_{O}^{\text{bind}} \geq 1 \).

The visual information in Figure 3(a) can be quantitatively analyzed by plotting the fractional distributions of \( N_{O}^{\text{bind}} \) as shown in Figure 3(b). When the water content is small as \( \phi_{W_t} = 0.1 \), most Li\(^+\) strongly interact with the polymers, and the majority of Li\(^+\) have a binding index of \( N_{O}^{\text{bind}} = 3 \) or \( 4 \). In such a low water content, the PAA polymer chains are deformed so that the Li\(^+\) can be easily bound to the multiple COO\(^-\) segments. When water is added, the polymer chains unfold, and the binding with the oxygen atoms from different PAA chains gets disturbed. For instance, for \( N_{O}^{\text{bind}} = 3 \), every oxygen atom comes one by one from adjacent monomers in the same PAA chain (see Figure 3(a)). For the unfolded polymer, the water molecules can easily intervene in the Li\(^+\)–O pair, weakening the binding by increasing the Li\(^+\)–O distance, and eventually, the \( N_{O}^{\text{bind}} \) of that Li\(^+\) is reduced. First, the decrease of the binding with \( N_{O}^{\text{bind}} = 3 \), \( 4 \) transferred to the bindings with \( N_{O}^{\text{bind}} = 2 \) (\( 0.1 \leq \phi_{W_t} \leq 0.4 \)). Then, the fraction of \( N_{O}^{\text{bind}} = 0 \) grew until saturation (\( 0.5 \leq \phi_{W_t} \leq 0.7 \)). The change in the fraction of \( N_{O}^{\text{bind}} = 1 \) is not considerable. Because the two oxygen atoms are located close to each other in one monomer unit, the binding with \( N_{O}^{\text{bind}} = 2 \) is preferred as opposed to the single-oxygen binding (\( N_{O}^{\text{bind}} = 1 \)). Overall, it can be said that the release of Li ions happens like the jumps with a step size of 2: When \( N_{O}^{\text{bind}} \) is reduced from 4 to 0, its process is \( 4 \rightarrow 2 \rightarrow 0 \), not \( 4 \rightarrow 3 \rightarrow 2 \rightarrow 1 \rightarrow 0 \). For high water content with \( \phi_{W_t} \geq 0.7 \), the \( N_{O}^{\text{bind}} \) distribution remains unchanged, which corresponds to the sudden slow-down of increment of the conductivity in the structure-dominant regime (see Figure 2(a)).

4.3. Diffusion of Li Ion. Figure 4(a) shows the fractions of bound and free Li\(^+\) as a function of water content. Initially (when \( \phi_{W_t} = 0.1 \)), most Li\(^+\) were bound to the PAA polymer. In the diffusion-dominant regime (\( \phi_{W_t} < 0.7 \)), with the addition of water, the fraction of bound Li\(^+\), \( \phi_{W_t}^{\text{bound}} \), decreases from 0.99997 at \( \phi_{W_t} = 0.1 \) to 0.8554 at \( \phi_{W_t} = 0.7 \), whereas the fraction of free Li\(^+\), \( \phi_{W_t}^{\text{free}} \), is on the rise from 3.23 \times 10^{-7} at \( \phi_{W_t} = 0.1 \) to 0.1446 at \( \phi_{W_t} = 0.7 \). In the structure-dominant regime (\( \phi_{W_t} \geq 0.7 \)), the changes in \( \phi_{W_t}^{\text{bound}} \) and \( \phi_{W_t}^{\text{free}} \) become slower. Hence, the maximum \( \phi_{W_t}^{\text{free}} \)-value achieves only 0.1955, even in a very high-water-content environment (\( \phi_{W_t} = 0.9 \)). These observations suggest that the interaction between the polymer and Li\(^+\) is strong enough to overwhelm the solvation-induced attraction toward the outer water-rich zone. The solvation-induced attraction is induced by the tendency of ions to be solvated in bulk water. Thus, even with sufficient water, a large
number of Li\(^+\) remain near the polymer. Of course, some Li\(^+\) escape the binding area to become free ions, as seen in the change of \(\phi_{Wt}\).

Figure 4(b) compares the diffusion coefficients of free and bound Li\(^+\). Both diffusion coefficients increase steadily as the amount of water in the system increases. However, the contributions of free and bound Li\(^+\) on the total Li\(^+\) diffusion should be identified with \(\phi_{Li}^{free} D_{Li}^{free}\) and \(\phi_{Li}^{bound} D_{Li}^{bound}\), because the total Li\(^+\) diffusion coefficient, \(D_{Li}\), is given as \(D_{Li} = \phi_{Li}^{free} D_{Li}^{free} + \phi_{Li}^{bound} D_{Li}^{bound}\). As seen in Figure 4(c), the contribution of free Li\(^+\) is 10\(^4\) times smaller than that of bound Li\(^+\) at \(\phi_{Wt} = 0.1\), the increment of \(\phi_{Li}^{free} D_{Li}^{free}\) according to \(\phi_{Wt}\) is much faster than the rising rate of \(\phi_{Li}^{bound} D_{Li}^{bound}\). Then, \(\phi_{Li}^{bound} D_{Li}^{bound}\) becomes identical to \(\phi_{Li}^{free} D_{Li}^{free}\) at \(\phi_{Wt} \approx 0.7\). For the bound Li\(^+\), the contribution steadily increases in proportion to \(\phi_{Wt}\) across the entire range of \(\phi_{Wt}\), which can be fitted with a single line (see eq S2). However, increasing rate of the contribution of free Li\(^+\) considerably decreases with increasing \(\phi_{Wt}\), so that the entire \(\phi_{Li}^{free} D_{Li}^{free}\) profile can be fitted with three distinctive straight lines (see eq S3). In summary, for \(\phi_{Wt} < 0.7\), the bound Li\(^+\) govern the ion conductivity, while for \(\phi_{Wt} \geq 0.7\), the conductivity is attributable to both free and bound Li\(^+\).

Although the conventional study based on free and bound ions unveiled many details in the transport of Li\(^+\) through the PAA–Li\(^+\)–water electrolyte, we still had fundamental questions as follows: (1) Why do the diffusion coefficients increase steadily throughout the entire range of water content, while \(\phi_{Li}^{free}\) and \(\phi_{Li}^{bound}\) are saturated in the structure-dominant regime? (2) What is the physical meaning of \(\phi_{Wt} = 0.7\), at which the contribution of free Li\(^+\) becomes identical to that of bound Li\(^+\)? We felt that these questions could be answered by investigating the ion and water structures around the polymer and their interplay. Next, we focus on the structural properties of the PAA–Li\(^+\)–water electrolyte (i.e., microstructures of Li\(^+\) and water around PAA). As mentioned before, the microstructures are closely correlated with \(n_{Li}\).

### 4.4. Ion and Water Structure around Polymer

Figure 5 presents the number density distributions of Li\(^+\) and water around a PAA monomer, respectively. Overall, with an increase in \(\phi_{Wt}\), \(n_{Li}\) decreases, whereas the number density of water, \(n_{Wt}\), increases. As mentioned already, the simulation box expanded with the addition of water, which caused an overall decrease in the number density of Li\(^+\) and \(n_{Li}\). However, for \(n_{Wt}\), the increase in the number of water molecules was more influential than the change in volume; thus, \(n_{Wt}\) increased. The changes in \(n_{Li}\) and \(n_{Wt}\) were considerably lessened in the structure-dominant regime \((\phi_{Wt} \geq 0.7)\). For Li\(^+\), the density at the second peak \((r \approx 0.5 \text{ nm})\) dropped from 12.62 nm\(^{-3}\) at \(\phi_{Wt} = 0.1\) to 4.60 nm\(^{-3}\) at \(\phi_{Wt} = 0.9\), while the bulk density \((r > 1.2 \text{ nm})\) was reduced from 11.00 nm\(^{-3}\) at \(\phi_{Wt} = 0.1\) to 1.00 nm\(^{-3}\) at \(\phi_{Wt} = 0.9\). However, the effects of water addition on the first peak were not very important. In this case, \(n_{Li}\) at the first peak \((r \approx 0.24 \text{ nm})\) appeared as 30.90 nm\(^{-3}\) at \(\phi_{Wt} = 0.1\) and 25.06 nm\(^{-3}\) at \(\phi_{Wt} = 0.9\). These observations confirm that the Li\(^+\) in the first peak were tightly bound to the polymer so that they were not easily released, even though more water molecules were added. Instead, those additional water molecules pushed the Li ions in the first valley \((r \approx 0.36 \text{ nm})\) to the bulk, causing a 10-fold decrease in the Li-ion density at \(r \approx 0.36 \text{ nm}\) \((n_{Li} = 3.55 \text{ nm}^{-3})\) at \(\phi_{Wt} = 0.1\) and \(n_{Li} = 0.41 \text{ nm}^{-3}\) at \(\phi_{Wt} = 0.9\).
Figure 6. (a) Change of diffusion coefficients of PAA monomer and water depending on water content, $\phi_{Wt}$. (b) Correlation between the dynamics of water and the diffusional motion of the PAA monomer. $D_{\text{mon}}$ is the diffusion coefficient of the PAA monomer. (c) Correlation between the dynamics of the bound lithium ion, $D_{\text{Li, bound}}$, and the diffusional motion of the PAA monomer, $D_{\text{mon}}$.

Figure 7. (a) $N_{Wt}$ distributions for inner Li$^+$ depending on water contents of $\phi_{Wt} = 0.1, 0.3, 0.7$, and 0.9. Complete set of distributions for $0.1 \leq \phi_{Wt} \leq 0.9$ is given in Figure S13. (b) $N_{Wt}$ distributions for outer Li$^+$ depending on water content with $\phi_{Wt} = 0.1, 0.3, 0.7$, and 0.9. A complete set of distributions for $0.1 \leq \phi_{Wt} \leq 0.9$ is given in Figure S14. (c) Variation of average hydration number for inner Li$^+$ (left) and outer Li$^+$ (right) according to $\phi_{Wt}$. Different colors express the contributions from inner and outer water.
Different from $n_{Li}$ in the first peak, $n_{Li}$ in the second peak was readily influenced by the water addition, because the binding by PAA chains is weak.

The responses of $n_{Wt}$ to water addition are opposite to those of $n_{Li}$ (i.e., $n_{Wt}$ increased uniformly across the entire domain as $\phi_{Wt}$ increases). At the second peak ($r \approx 0.62$ nm), $n_{Wt}$ increased from 5.74 nm$^{-3}$ at $\phi_{Wt} = 0.1$ to 27.68 nm$^{-3}$ at $\phi_{Wt} = 0.9$, while $n_{Wt}$ in the bulk region ($r > 1.2$ nm) rose from 5.28 nm$^{-3}$ at $\phi_{Wt} = 0.1$ to 30.93 nm$^{-3}$ at $\phi_{Wt} = 0.9$. The second peak was imperceptible initially in the low-water-content condition but grew rapidly with the addition of water. Moreover, the first peak ($r \approx 0.39$ nm), which was initially a small bump in the profile, grew from 9.83 nm$^{-3}$ at $\phi_{Wt} = 0.1$ to 33.13 nm$^{-3}$ at $\phi_{Wt} = 0.9$. Despite those considerable changes in magnitude, the peak and valley positions in $n_{Li}$ and $n_{Wt}$ varied little with $\phi_{Wt}$. This can be clearly recognized by looking at the radial distribution functions (RDFs) for $Li^+$ and water together (see Figure S11). From Figure S11, we find that the peak and valley positions are preserved regardless of the addition of water. The $Li^+$-rich region and water-rich zone alternate around PAA, as schematically displayed in Figure 5(c). First, the positive $Li^+$ attach to the negative COO$^-$ in the PAA monomer due to strong electrostatic attraction. Then, the water molecules become arranged outside the $Li^+$-rich zone with the oxygen atoms oriented toward the $Li^+$. In the immediate vicinity of the polymer, the $Li^+$ and water molecules cannot be located very close to each other due to geometric hindrance by finite ion size.

Figure 5(d) shows an average equilibrium distance of $Li^+$ from the center of a PAA monomer according to $N_{bind}^{free}$. All the distances varied little except the case with $N_{bind}^{free} = 0$. In other words, the initial positions of bound $Li^+$ determined in a low-water-content environment are affected little by water addition. This yields the location-fixed first peaks in Figure 5(a). However, the equilibrium distance of the $Li^+$ located away from the polymer ($N_{bind}^{free} = 0$) rapidly increases with the addition of water, because the strong solvation tendency pushes the ions toward the bulk. This observation implies that once the $Li^+$ are properly coordinated with PAA polymer, they are not easily released from their binding sites (i.e., the PAA–$Li^+$ interaction is stronger than the solvation tendency of $Li^+$).

Here, we need to introduce the concepts of inner water and outer water. In the present study, the water inside the first hydration shell of polymer is called inner water, while the water outside the first shell is referred to as outer water. The inner and outer water each have a number of features (see Figure 6(a)). Because fully hydrated $Li^+$ has $N_{Wt} = 0.1$, the fractions are given as $\phi_{Wt,i}^{i} / \phi_{Wt}^{avg} = 0.641:0.300:0.053$, where $\phi_{Wt}^{i}$ is the fraction of the inner water with $N_{Wt} = i$ (see Figure 7(a)). In such a low-water-content environment, the majority of $Li^+$ was completely absorbed without any intervention of water molecules ($N_{Wt} = 0$). With the addition of water, $\phi_{Wt}^{i}$ significantly increases as $\phi_{Wt}^{i}$ decreases: at $\phi_{Wt} = 0.7$, the distribution appears to be $\phi_{Wt,3}^{i} / \phi_{Wt}^{avg} = 0.190:0.417:0.308$. Namely, the inner $Li^+$ ions without surrounding water acquire two water molecules at once upon the addition of water. This implies that for the $Li^+$ with $N_{Wt} = 0$, it is more energetically favorable to coordinate two water molecules than one. The coordination with $N_{Wt} > 2$ is hardly permitted because of the geometric hindrance. Noticeably, the $Li^+$ with $N_{Wt} = 1$ always remain in the majority over the other types of ions except in the case of $\phi_{Wt} = 0.1$. Figure 7(b) presents the $N_{Wt}$ distribution for outer $Li^+$. At $\phi_{Wt} = 0.1$, $\phi_{Wt}^{2} / \phi_{Wt}^{avg} = 0.313:0.533:0.122:0.032$. With the addition of water to $\phi_{Wt} = 0.3$, $\phi_{Wt}^{2}$ increased as $\phi_{Wt}^{4}$ and $\phi_{Wt}^{6}$ decreased. The fraction with $N_{Wt} = 4$ started to increase rapidly at $\phi_{Wt} = 0.3$, where the sudden changes in $\phi_{Wt}^{4}$ and $\phi_{Wt}^{6}$ start (see Figure 4(a)). Because fully hydrated $Li^+$ has $N_{Wt} = 4^{11,12}$, the increment in $\phi_{Wt}^{4}$ can be interpreted as that more and more ions have a bulk-like environment (see Figure 3(a)). The increment became remarkably slower in the structure-dominant regime.

Figure 7(c) compares the average hydration numbers, $N_{Wt}^{avg}$, for inner and outer $Li^+$. The portions of pink and cyan colors express the contributions of inner and outer waters, respectively, to $N_{Wt}^{avg}$. In the figure, $N_{Wt}^{avg}$ becomes saturated at 1.30 at $\phi_{Wt} = 0.5$ for inner $Li^+$, while $N_{Wt}^{avg}$ achieves 3.73 at $\phi_{Wt} = 0.6$ for outer $Li^+$. The small $N_{Wt}^{avg}$ explains the slow diffusion of inner $Li^+$, because $N_{Wt}^{avg}$ represents the mean number of water molecules colliding with ions to induce random motion of ions. Moreover, the inner $Li^+$ are mostly surrounded by the slower-moving inner waters.

Different from the inner $Li^+$, the outer $Li^+$ are affected by both inner and outer water. Initially, at $\phi_{Wt} = 0.1$ and 0.2, $N_{Wt}^{avg}$ is mostly determined by the inner water, because the $Li^+$ are so closely packed in the near vicinity of the polymer that their interaction with the outer water is weak. The average hydration number by inner water $N_{Wt}^{inw}$ ($r < 0.35$ nm), increases until $r$...
reaching the maximum at $\phi_{Wt} = 0.4$; it then decreases with a further increase in $\phi_{Wt}$. The hydration number of the faster-moving outer water, $N_{Wt}^{out,avg}$, which is negligible at $\phi_{Wt} = 0.1$ and 0.2, steadily increases with an increase in $\phi_{Wt}$ (starting...
from $\phi_{Wt \leq 0.3}$. This produced a steady increase in $D_{Li}^{free}$ outside the first hydration shell regardless of the saturation of the fraction of free Li$^+$ (see Figure 4(a)). Here, it should be noted again that the free Li$^+$ are mostly placed outside the first hydration shell. However, even at a very high water content ($\phi_{Wt \geq 0.9}$), $D_{Li}^{free}$ did not reach the value at infinite dilution in water,11,12 because the contribution of the slower inner water did not vanish completely.

4.6. Ion Migration Mechanism. In order to further understand the transport mechanism of Li$^+$ in the present electrolyte, we visualized the migration of a typical Li$^+$ through medium under an electric field of $E = 0.01$ V/nm for $\phi_{Wt} = 0.7$. The movie file is presented in the Supporting Information. The snapshots of the movie are also shown in Figure 8. In the figure, we can clearly observe that a water channel is formed,54 which acts as a passage for ion transport. As seen in the movie and the snapshots, at the high-water-content condition, a Li$^+$ ion bound to the oxygen atoms in the PAA polymer is released from the polymer by hydration to form a free ion (releasing process), travels the water channel freely, and is then trapped again by another PAA polymer (trapping process). Those releasing and trapping processes at high water content are shown in Figure 9. Different from the process at high water content, when the water content is low as $\phi_{Wt} = 0.3$, the lithium ions travel by jumping from one to another PAA polymer chains without solvation in water (see Figure 10).55 However, as the water is added and $\phi_{Wt}$ increases, the role of water becomes significant: The bound ion is released by hydration, and the free ion travels the water tube with large mobility.

The proposed electrolyte may have a low electrochemical window due to the larger water content. However, in the present study, we focused on a molecular-level understanding of the structural (ion/water distribution around the polymer) and dynamic (diffusion coefficient) properties of the PAA-based APE to develop highly conducting, flexible, and stable electrolytes. With the knowledge of how to design the high-conductivity APE, the addition of lithium salt to the electrolyte (such as a water-in-salt APE) can be one of the ways to increase an electrochemical window of the APE-based energy storage device. We have found that the lithium-salt incorporation leads to a further increase in ionic conductivity, as indicated by Suo et al.7 A full experimental and computational report on the electrochemical properties of the lithium-salt-containing APE-based energy storage device will be detailed in a forthcoming publication.

5. CONCLUSIONS

In conclusion, based on experiments and extensive MD simulations, we found that the conductivity of the polymer–Li$^+$–water electrolyte was able to increase to about $10^{-2}$ S/cm by employing strongly hydrophilic PAA as its polymer matrix, functionalizing lithium cations as mobile ions, and making the water content optimal. The change in conductivity according to $\phi_{Wt}$ was divided into the diffusion-dominant regime at the low-water-content condition ($\phi_{Wt} < 0.7$) and the structure-dominant regime at the high-water-content condition ($\phi_{Wt} \geq 0.7$). In the diffusion-dominant regime, the conductivity was increased by diffusion enhancement proportional to the water content, while in the structure-dominant regime, the conductivity varied little due to the considerable reduction of the number density of Li$^+$. The rigorous understanding of the steady increase in free and bound ion diffusions and the constant decrease in the number density of Li$^+$ across the entire $\phi_{Wt}$ range was possible only when the microscopic interaction between ions, water, and polymers was considered instead of the classical approach based on free ions.24 When water was introduced, the added water went to both the outside and the inside of the first hydration shell of PAA. The inner Li$^+$ were always dissolved in the slower inner water (inside the first hydration shell of polymer), and $N_{Wt}^{in}$ was increased to 1.3. However, for the outer Li$^+$, the fraction of the fast-moving outer water in their surroundings rapidly increased as $\phi_{Wt}$ increased, and $N_{Wt}^{out}$ became close to 4. Such strong hydration with faster-moving water brought about the gigantic increase in the outer, and subsequently total, ion diffusion. At $\phi_{Wt} = 0.7$, the fraction of inner water became identical with that of outer water. For $\phi_{Wt} < 0.7$, PAA polymer was able to absorb water, and as a result, the electrolyte's structural characteristics including $N_{Wt}^{in}$, $\phi_{Li}^{bound/free}$, and $N_{Wt}^{out}$ were altered according to $\phi_{Wt}$. For $\phi_{Wt} \geq 0.7$, the amount of water exceeded the polymer’s water absorption capacity and the excess waters in the outer region did not interact with the ion–water structure near the polymer. This caused the system volume to expand and the ion number density to shrink considerably.

Considering that the structural stiffness of APE could be weakened by the addition of water, the observations in the present study will be greatly helpful in optimizing water content to achieve a rigid electrolyte while maximizing its conductivity. Also, the proposed PAA-based APE may not be used for Li metal batteries due to the electrolyte containing water. However, the APE can be used as an electrolyte for an aqueous rechargeable lithium-ion battery (ARLB), which was invented in 1994 using an aqueous electrolyte, a LiMn$_2$O$_4$ cathode, and a VO$_2$(B) anode.56 Therefore, the proposed nontoxic and flexible APE could offer a promising solution for the development of flexible and wearable aqueous rechargeable lithium-ion batteries that would have wide applications in displays, wireless sensors, and implantable medical devices.7

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsaem.0c01765.

Ionic conductivity measurement, size of vinyl silica nanoparticles (VSNs), extent of neutralization with lithium cations in the electrolyte, compositions of polymer, nanoparticle, and water, molecular weight and lengths of PAA strands between nanoparticles, glass transition temperature, silica nanoparticle distribution within PAA matrix, pH measurement, validity of Nernst– Einstein equation, line fits, MSD plots, distribution of $N_{O}$, RDFs of Li$^+$ and water around a PAA monomer, inner vs. outer water, distribution of $N_{Wt}$, distribution of $N_{Wt}$ (PDF)

Migration of a typical Li$^+$ through medium under an electric field of $E = 0.01$ V/nm for $\phi_{Wt} = 0.7$ (MP4)

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Notes
The authors declare no competing financial interest.

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